Lecture No.13 Binary Tree Traversal - II

CC-213 Data Structures Department of Computer Science University of the Punjab

Slides modified very slightly from the late Dr. Sohail Aslam's lectures at VU

- There is yet another way of traversing a binary tree that is not related to recursive traversal procedures discussed previously.
- In level-order traversal, we visit the nodes at each level before proceeding to the next level.
- At each level, we visit the nodes in a leftto-right order.



Level-order: 14 4 15 3 9 18 7 16 20 5 17

- How do we do level-order traversal?
- Surprisingly, if we use a queue instead of a stack, we can visit the nodes in level-order.
- Here is the code for level-order traversal:

void levelorder(TreeNode<int>* treeNode)

{

```
Queue<TreeNode<int>* > q;
if( treeNode == NULL ) return;
q.enqueue( treeNode);
while( !q.empty() )
{
    treeNode = q.dequeue();
    cout << *(treeNode->getInfo()) << " ";</pre>
    if(treeNode->getLeft() != NULL )
          q.enqueue( treeNode->getLeft());
    if(treeNode->getRight() != NULL )
          q.enqueue( treeNode->getRight());
}
cout << endl;</pre>
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cout << endl;</pre>



Queue: 14 Output:



Queue: 4 15 Output: 14



Queue: 15 3 9 Output: 14 4



Queue: 3 9 18 Output: 14 4 15



Queue: 9 18 Output: 14 4 15 3



Queue: 18 7 Output: 14 4 15 3 9



Queue: 7 16 20 Output: 14 4 15 3 9 18



Queue: 16 20 5 Output: 14 4 15 3 9 18 7



Queue: 20 5 17 Output: 14 <u>4 15 3 9 18 7 16</u>



Queue: 5 17 Output: 14 4 15 3 9 18 7 16 20



Queue: 17 Output: 14 <u>4 15 3 918 716 205</u>



Queue: Output: 14 4 15 3 9 18 7 16 20 5 17

Storing other Type of Data

- The examples of binary trees so far have been storing integer data in the tree node.
- This is surely not a requirement. Any type of data can be stored in a tree node.
- Here, for example, is the C++ code to build a tree with character strings.

void wordTree()

TreeNode<char>* root = new TreeNode<char>(); static char* word[] = {"babble", "fable", "jacket", "backup", "eagle", "daily", "gain", "bandit", "abandon", "abash", "accuse", "economy", "adhere", "advise", "cease", "debunk", "feeder", "genius", "fetch", "chain", NULL}; root->setInfo(word[0]);

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for(i=1; word[i]; i++ )
     insert(root, word[i] );
inorder( root ); cout << endl;</pre>
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{
       TreeNode<char>* node = new TreeNode<char>(info);
       TreeNode<char> *p, *q;
       p = q = root;
       while( strcmp(info, p->getInfo()) != 0 && q != NULL )
       {
            \mathbf{p} = \mathbf{q};
            if( strcmp(info, p->getInfo()) < 0 )</pre>
                 q = p - > getLeft();
            else
                q = p - getRight();
       }
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if( strcmp(info, p->getInfo()) == 0 ){
    cout << "attempt to insert duplicate: " << *info
        << endl;
      delete node;
    }
    else if( strcmp(info, p->getInfo()) < 0 )
      p->setLeft( node );
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Output: abandon abash accuse adhere advise babble backup bandit cease chain daily debunk eagle economy fable feeder fetch gain genius jacket

abandon abash accuse adhere advise babble backup bandit cease chain daily debunk eagle economy fable feeder fetch gain genius jacket

 Notice that the words are sorted in increasing order when we traversed the tree in inorder manner.

abandon abash accuse adhere advise babble backup bandit cease chain daily debunk eagle economy fable feeder fetch qain genius jacket

- Notice that the words are sorted in increasing order when we traversed the tree in inorder manner.
- This should not come as a surprise if you consider how we built the BST.

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- For a given node, values less than the info in the node were all in the left subtree and values greater or equal were in the right.

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- Inorder prints the left subtree, then the node finally the right subtree.

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- Building a BST and doing an inorder traversal leads to a sorting algorithm.

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- Building a BST and doing an inorder traversal leads to a sorting algorithm.

- As is common with many data structures, the hardest operation is deletion.
- Once we have found the node to be deleted, we need to consider several possibilities.
- If the node is a *leaf*, it can be deleted immediately.

If the node has one child, the node can be deleted after its parent adjusts a pointer to bypass the node and connect to inorder successor.



 The inorder traversal order has to be maintained after the delete.



 The inorder traversal order has to be maintained after the delete.



- The complicated case is when the node to be deleted has both left and right subtrees.
- The strategy is to replace the data of this node with the smallest data of the right subtree and recursively delete that node.

Delete(2): locate inorder successor



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- Inorder successor will be the left-most node in the right subtree of 2.
- The inorder successor will not have a left child because if it did, that child would be the left-most node.

Delete(2): copy data from inorder successor



Delete(2): remove the inorder successor



Delete(2)

