# **CS-568** Deep Learning

Long Short-Term Memory (LSTM)

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# Weakness of standard RNN

- We have already seen that RNNs do not possess long-term memory.
- lnput at time t is soon forgotten because of the recurrent weights  $W^{11}$ .
- Would be nice to decide what and how much to forget/remember based on the input itself.



#### Long Short-Term Memory (LSTM) Building blocks

Let 
$$\mathbf{v}^{(t)} = \begin{bmatrix} \mathbf{h}^{(t-1)} \\ \mathbf{x}^{(t)} \end{bmatrix} \in \mathbb{R}^{(M+D) \times 1}$$

Perform 4 affine transformations of  $v^{(t)}$  followed by non-linearities.

$$\mathbf{f}^{(t)} = \sigma \left( W_f \mathbf{v}^{(t)} + \mathbf{b}_f \right) \tag{1}$$

$$\mathbf{i}^{(t)} = \sigma \left( W_i \mathbf{v}^{(t)} + \mathbf{b}_i \right)$$
(2)

$$\mathbf{o}^{(t)} = \sigma \left( W_o \mathbf{v}^{(t)} + \mathbf{b}_o \right) \tag{3}$$

$$\tilde{\mathbf{c}}^{(t)} = \tanh\left(W_c \mathbf{v}^{(t)} + \mathbf{b}_c\right) \tag{4}$$

All 4 matrices of size  $M \times (M + D)$  and therefore all 4 transformations produce *M*-dimensional vectors.

Vectors  $\mathbf{f}^{(t)}, \mathbf{i}^{(t)}, \mathbf{o}^{(t)}$  contain values in (0, 1) and  $\tilde{\mathbf{c}}^{(t)}$  in (-1, 1).

### **LSTM** *Putting everything together*



LSTM Cell: Operations at the hidden layer.

- Vector c<sup>(t)</sup> is interpreted as the cell state.
- Cell state is recurrent as well.
- Notice that  $\mathbf{c}^{(t)}$  is not forced to contain values in (0, 1) or (-1, 1).

#### Gates

# Role of the Gates $f^{(t)}$ : Forget Gate

$$\mathbf{f}^{(t)} = \sigma \left( W_f \mathbf{v}^{(t)} + \mathbf{b}_f \right)$$
$$c_j^{(t)} = f_j^{(t)} c_j^{(t-1)} + i_j^{(t)} \tilde{c}_j^{(t)}$$

 $\mathbf{f}^{(t)}$  acts as a forget gate on the previous cell state  $\mathbf{c}^{(t)}$ .

#### Gates

# Role of the Gates $\mathbf{i}^{(t)}$ : Input Gate

$$\mathbf{i}^{(t)} = \sigma \left( W_i \mathbf{v}^{(t)} + \mathbf{b}_i \right)$$
$$c_j^{(t)} = f_j^{(t)} c_j^{(t-1)} + i_j^{(t)} \tilde{c}_j^{(t)}$$

 $\mathbf{i}^{(t)}$  acts as an input gate on the potential cell state  $\mathbf{\tilde{c}}^{(t)}$ .

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### **Role of the Gates** o<sup>(t)</sup>: Output Gate

$$\mathbf{o}^{(t)} = \sigma \left( W_o \mathbf{v}^{(t)} + \mathbf{b}_o \right)$$
$$h_j^{(t)} = o_j^{(t)} \tanh(c_j^{(t)})$$

 $\mathbf{o}^{(t)}$  acts as an output gate on  $\mathbf{c}^{(t)}$ .

## **LSTM**



LSTM Cell: Operations at the hidden layer in detail.

# Information flow

- Depending on f<sup>(t)</sup> and i<sup>(t)</sup>, an LSTM cell has the ability to push through its cell state c<sup>(t-1)</sup> exactly or almost unchanged into the next time step c<sup>(t)</sup>.
- This ensures flow of the cell state (memory) through time. Hence long-term memory.
- This is similar to how other deep learning techniques ensure flow of information in space.
  - ReLU
  - Weight initialization
  - Batchnorm
  - Residual block

# Remembering the past

• Consider a sentence containing brackets.

England (last year's winners) are expected to put up a good fight.

- The LSTM cell can learn to set c<sub>j</sub> = 1 if an opening bracket is seen at time t.
- ▶ It can also learn to keep  $c_j = 1$  for a long time until a closing bracket is seen *in the input*.
- Some other  $c_k$  can similarly be used to handle nested brackets and so on.
- Even the value of c<sub>j</sub> itself can be used to signify the level of nesting. It all depends on how and what the LSTM learns.

# **Peephole Connections**

Allow gates to look at the cell state as well before deciding what to forget, what to add, and what to output.

$$\mathbf{v}_{f,i}^{(t)} = \begin{bmatrix} \mathbf{c}^{(t-1)} \\ \mathbf{h}^{(t-1)} \\ \mathbf{x}^{(t)} \end{bmatrix} \in \mathbb{R}^{(2M+D) \times 1}$$
$$\mathbf{v}_{o}^{(t)} = \begin{bmatrix} \mathbf{c}^{(t)} \\ \mathbf{h}^{(t-1)} \\ \mathbf{x}^{(t)} \end{bmatrix} \in \mathbb{R}^{(2M+D) \times 1}$$

# Coupled forget and input

► Use a single forget gate for interpolation.

$$\mathsf{c}^{(t)} = \mathsf{f}^{(t)} \odot \mathsf{c}^{(t-1)} + (1 - \mathsf{f}^{(t)}) \odot \tilde{\mathsf{c}}^{(t)}$$

Fewer parameters due to removal of input gate.

# Gated Recurrence Unit (GRU)

- Coupled forget and input gates.
- Merged hidden and cell state.

$$\mathbf{z}^{(t)} = \sigma \left( W_z \mathbf{v}^{(t)} + \mathbf{b}_z \right)$$
$$\mathbf{r}^{(t)} = \sigma \left( W_r \mathbf{v}^{(t)} + \mathbf{b}_r \right)$$
$$\tilde{\mathbf{h}}^{(t)} = \tanh \left( W_h[\mathbf{r}^{(t)} \odot \mathbf{h}^{(t-1)}; \mathbf{x}^{(t)}] + \mathbf{b}_h \right)$$
$$\mathbf{h}^{(t)} = \left( 1 - \mathbf{z}^{(t)} \right) \odot \mathbf{h}^{(t-1)} + \mathbf{z}^{(t)} \odot \tilde{\mathbf{h}}^{(t)}$$

- Always expose the hidden state.
- In some variants, the weight matrices can be set to 0.
- In other variants, the bias vectors can be set to 0.
- Fewer parameters, faster training, learning from lesser data.

### Summary

- RNNs do not retain long-term context in practice.
- An LSTM cell has the ability to push through its cell state exactly or almost unchanged into the next time step.
- This ensures flow of the cell state (memory) through time. Hence long-term memory.