# CS-568 Deep Learning

Nazar Khan

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Convolutional Neural Networks

Neurons as Detectors

CNN

Convolutional layer

Subsamplin

FC Layers

# Convolution

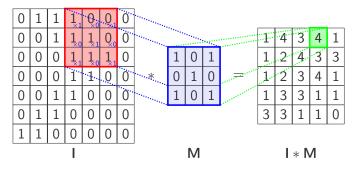
Source: http://www.texample.net/tikz/examples/convolution-of-two-functions/

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#### **2D Convolution** *Example*



 $Modified \ from \ \texttt{https://github.com/PetarV-/TikZ/tree/master/2D\%20Convolution}$ 

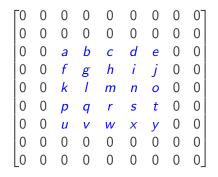
*M* is usually called a *mask* or *kernel* or *filter*.

# Dealing with boundaries

- What about edge and corner pixels where the mask goes outside the image boundaries?
  - Expand image *I* with virtual pixels. Options are:
    - 1. Fill with a particular value, e.g. zeros.
    - 2. Replicating boundaries: fill with nearest pixel value.
    - 3. Reflecting boundaries: mirror the boundary
  - Fatalism: just ignore them. Not recommended since size of *I* \* *M* will shrink.

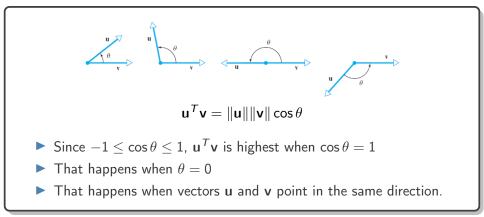
#### **Dealing with boundaries** *Expand by zeros*

#### For a 5 $\times$ 5 image and 5 $\times$ 5 mask



#### A Neuron as a Detector

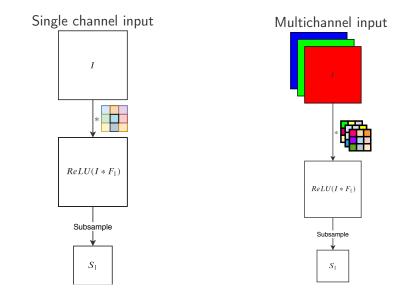
- A neuron can be viewed as a detector.
- When it fires, the input must have been similar to its weights.
  - Firing  $\implies \mathbf{w}^T \mathbf{x}$  was high  $\implies \mathbf{w}$  was similar to  $\mathbf{x}$
- So neuron firing indicates detection of something similar to its weights.



## **Convolutional Neural Networks**

- Now we will look at networks that produce neuronal output via convolution.
- Known as Convolutional Neural Networks (CNNs).
- Most frequently used network architecture.
- Exploits local correlation of inputs.

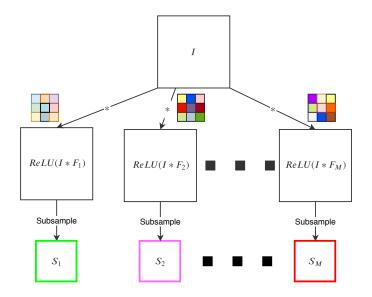
#### Building Blocks of CNNs Viewing convolution as neurons



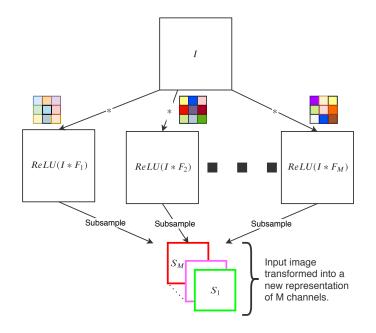
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## Building blocks of CNNs



## Building blocks of CNNs



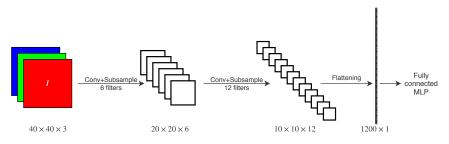
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#### **CNN**

- Convolution by *M* filters produces *M* channels.
- ▶ They represent an *M*-channel transformation of the input image *I*.
- This *M*-channel image can now be transformed further via additional convolution filters.
- Convolution-subsampling block can be repeated multiple times.
- ▶  $I \rightarrow M_1$  channels  $\rightarrow M_2$  channels  $\rightarrow \cdots \rightarrow M_b$  channels  $\rightarrow$  flattening  $\rightarrow$  MLP.



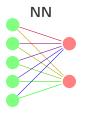
## **Convolutional Neural Networks**

- ▶ For recognition of hand-written digits, we have seen that inputs are images and outputs are posterior probabilities p(C<sub>k</sub>|x) for k = 1,...,10.
- The digits true identity is invariant under
  - translation, scaling, (small) rotation, and
  - small elastic deformations (multiple writings of the same digit by the same person will have subtle differences).
- The output of the neural network should also be invariant to such changes.
- A traditional fully connected neural network can, in principle, learn these invariances using lots of examples.

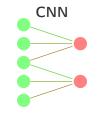
#### **Convolutional Neural Networks**

- ► However, it totally ignores the *local correlation* property of images.
  - ► Nearby pixels are more strongly correlated than pixels that are far apart.
- Modern computer vision exploits local correlation by extracting features from local patches and combines this information to detect higher-order features.
  - $\blacktriangleright \quad \mathsf{Example: Gradients} \longrightarrow \mathsf{Edges} \longrightarrow \mathsf{Lines} \longrightarrow \ldots$
- Local features useful in one sub-region can be useful in other sub-regions.
  - Example: same object appearing at different locations.
- This weakness of standard neural nets is overcome by CNNs.

## NN vs. CNN



- Global receptive fields due to being fully connected.
- Separate weights for each neuron.



- Local receptive fields due to being sparsely connected.
- Shared weights among different neurons.
- Subsampling of each layer's outputs.

Receptive field of a neuron consists of previous layer neurons that it is connected to (or looking at).

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#### **Convolutional layer**

- Consists of multiple arrays of neurons. Each such array is called a *slice* or more accurately *feature map*.
- Each neuron in a feature map
  - ▶ is connected to only few neurons in the previous layer, but
  - uses the same weight values as all other neurons in that feature map.
- So within a feature map, we have both
  - local receptive fields, and
  - shared weights.

#### **Convolutional layer**

- Example: A feature map may have
  - ▶ 100 neurons placed in a  $10 \times 10$  array, with
  - each neuron getting input from a 5 × 5 patch of neurons in the previous layer (receptive field), and
  - the same  $26(=5 \times 5 + 1)$  weights shared between these 100 neurons.
- Viewed as detectors, all 100 neurons detect the same 5 × 5 pattern but at different locations of the previous layer.
- Different feature maps will learn<sup>1</sup> to detect different kinds of patterns.
  - For example, one feature map might learn to detect horizontal edges while others might learn to detect vertical or diagonal edges and so on.

<sup>&</sup>lt;sup>1</sup>based on their learned weights

### **Convolutional layer**

- To compute activations of the 100 neurons, a dot-product is computed between the same shared weights and different 5 × 5 patches of previous layer neurons.
- This is equivalent to sliding a window of weights over the previous layer and computing the dot-product at each location of the window.
- Therefore, activations of the feature map neurons are computed via convolution of the previous layer with a kernel comprising the shared weights. Hence the name of this layer.

# Subsampling layer

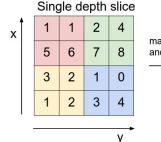
- Reduces the spatial dimensions of the previous layer by downsampling. Also called *pooling* layer.
- Example: downsampling previous layer of  $n \times n$  neurons by factor 2 yields a pooled layer of  $\frac{n}{2} \times \frac{n}{2}$  neurons.
- ► No adjustable weights. Just a fixed downsampling procedure.
- Reduces computations in subsequent layers.
- Reduces number of weights in subsequent layers. This reduces overfitting.

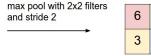
8

4

### Subsampling

- ▶ Options: From non-overlapping  $2 \times 2$  patches
  - pick top-left (standard downsampling by factor 2)
  - pick average (mean-pooling)
  - pick maximum (max-pooling)
  - pick randomly (stochastic-pooling)
  - Fractional max-pooling: pick pooling region randomly.





**Figure:** Max-pooling with 2 × 2 receptive fields, and stride of 2 neurons. Source: http://cs231n.github.io/convolutional-networks/

Convolutional layer

## Subsampling

- ▶ The options in the last slide discard 75% of the data.
- They correspond to
  - neurons with  $2 \times 2$  receptive fields, and
  - *stride* of 2 neurons.
- This is the most commonly used configuration. Other options exist but note that pooling with larger receptive fields discards too much data.
- Subsampling layer can be skipped if convolution layers uses stride>1 since that also produces a subsampled output.

# Subsampling

# A pooling layer

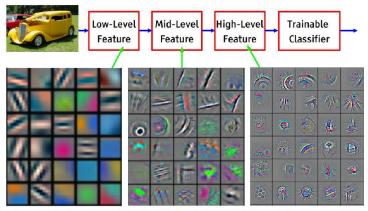
- with  $F \times F$  receptive field and stride *S*,
- "looking at" a  $W_1 \times H_1 \times D_1$  input volume,
- ▶ produces a  $W_2 \times H_2 \times D_2$  output volume, where

• 
$$W_2 = \frac{W_1 - F}{S} + 1$$
  
•  $H_2 = \frac{H_1 - F}{S} + 1$   
•  $D_2 = D_1$ .

# Fully Connected Layers

- ► After flattening, a fully connected MLP can be used.
- ► The last layer has
  - neurons equal to the desired output size, and
  - activation functions based on the problem to be solved.
- The flattened layer can therefore be viewed as a transformation φ(x) that is fed into an MLP.
- Similarly, outputs of earlier layers are *intermediate representations* of the input.

#### Intermediate Representations



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

Intermediate feature representations. Early layers form simple, low-level representations of the input. They are used to incrementally form more complex, high-level representations. Source: http://cs231n.stanford.edu/slides/winter1516\_lecture7.pdf

## **CNN Variations**

- ► There are *lots* of variations.
  - ▶ Fully convolutional networks. No pooling and no fully connected layer.
  - $1 \times 1$  convolutions to reduce computations.
  - Inception modules to combine multiple filter sizes.
  - Residual blocks to avoid vanishing gradients.
  - Depthwise separable convolutions to reduce parameters and computations.
  - Lightweight and fast models (SqueezeNet, MobileNet, ...) for edge computing.
  - Fast search over hyperparameters (EfficientNet).