

MA 120 Probability and Statistics

Prob.

Uncertainty
Randomness

Prob. uses statistics
to make predictions
or decisions in
uncertain scenarios.

Stats.

Summary of info.

L Avg - height of students in this class

(Max)

(Min)

⋮

Quantitative

Bar Chart



Pie Chart

Qualitative

Probability

$$2+3=5$$

$$4 \times 3 = 12$$

$$\text{Force} = \text{Mass} \times \text{Acceleration}$$

$$\text{Distance} = \text{Speed} \times \text{Time}$$

Pure
Perfect measurement
Water will boil at 100°C .

Deterministic Experiments

What will be the result of a coin toss? $\begin{cases} H \\ T \end{cases}$
Real world is noisy.

$$y = f(x) + \underbrace{\text{noise}}_{\substack{\text{uncertainty} \\ \text{randomness}}}$$

Random Experiment

Is a coin toss really random?

- If you understand & control the Physics of the coin toss, it's not random.
- Randomness is an acknowledgement of our ignorance.
- Human coin toss is random. It is too complex to understand & control.
 - is considered to be random. ← says nothing about reality.
 - a phenomenon might be actually random or it might be deterministic (but too complex).
 - If it is too complex, we will deal with it under the framework of randomness.
 - best approximation is to consider it to be random.
 - Randomness is a convenient term to express our ignorance of complex phenomena.
 - L Sub-atomic

Randomness vs. Chaos

- Chaos is when nothing can be predicted.
Most extreme form of randomness.
- Usually, randomness is less extreme.
"Some" predictions can be made.
- Randomness, just like Physics, has its own set of laws. Its own terminology.

Probability deals with such laws.

Terminology

① Random Experiment

- ↳ Exp. with uncertain output
- ↳ Trial

② Sample space (set of all possible outcomes)

$$S = \{H, T\}$$

2 coins $S = \{1, 2, 3, 4, 5, 6\}$

Venn Diagram

$$S = \{HH, HT, TH, TT\}$$



③ Event

Outcomes that we are interested in.

$$A = \{H\}$$

$$A = \{2, 4, 6\}$$

$$A = \{HH, HT\}$$

$$B = \{TH, TT\}$$

$$C = \{HT, TT\}$$

$$A^c = \{1, 3, 5\} \leftarrow \text{event}$$

$$B \cup C = \{TH, TT, HT\} \leftarrow \text{event}$$

$$B \cap C = \{TT\} \leftarrow \text{event}$$



④ Event Occurrence

$$A = \{2, 4, 6\}$$

"A occurs" means one of the elements of A was the outcome of the experiment.

$$P(\text{event}) = \text{likelihood of event}$$

How to assign $P(\text{events})$?

- ① Empirical Approach
- ② Counting Approach
- ③ Measuring "
- ④ Independence